

Transportable optical clocks



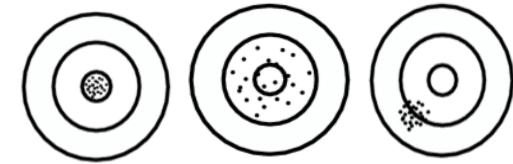
Christian Lisdat



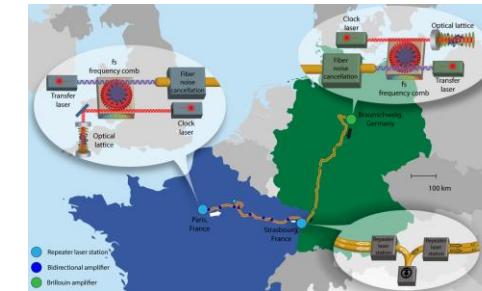
656th WE Heraeus Seminar 25.10.2017

Outline:

► Clock basics, Vocabulary



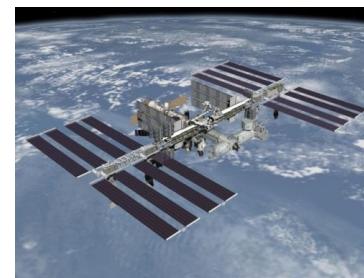
► Clocks in the lab: examples of experiments



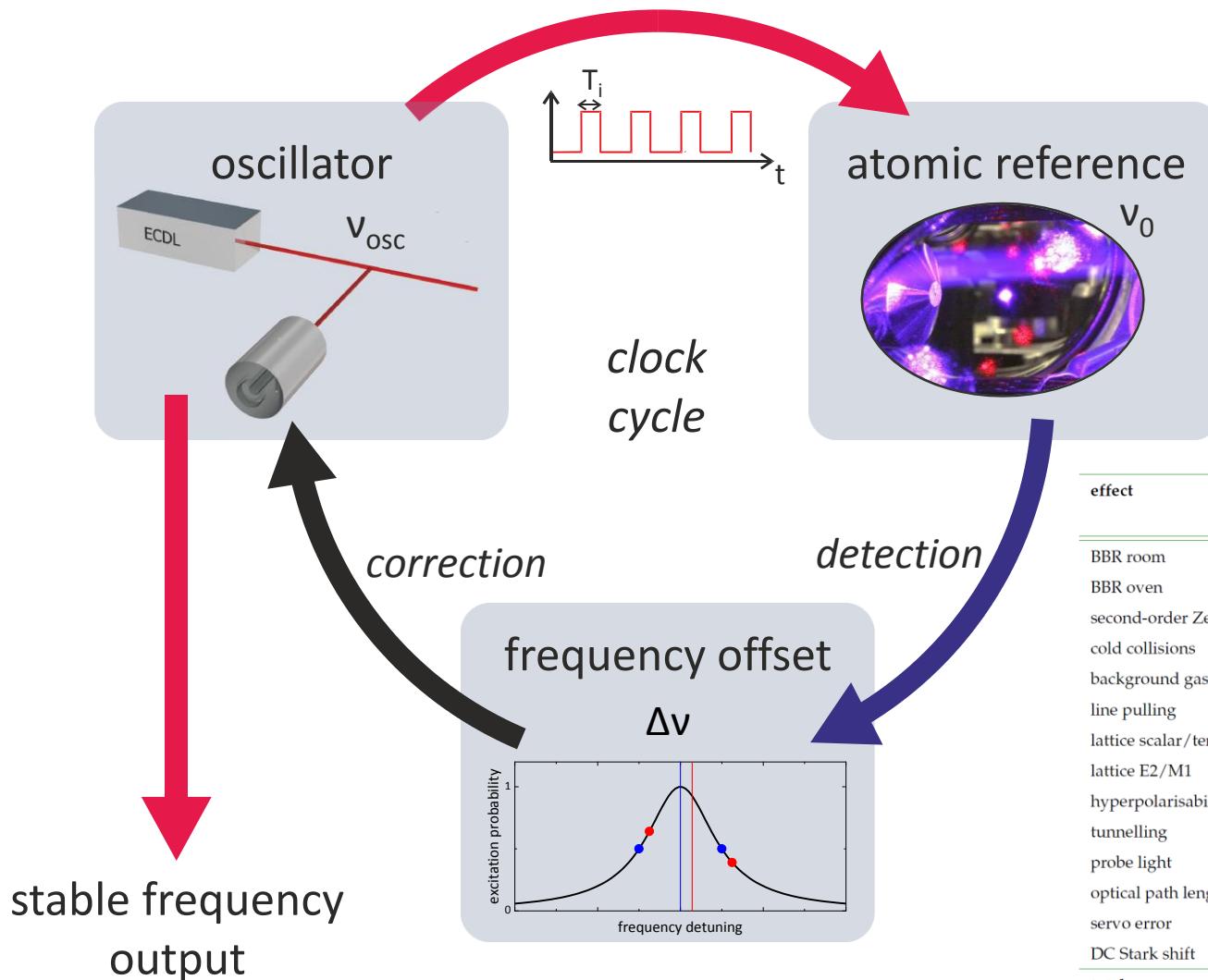
► Transportable optical clocks on ground



► Optical clocks in space



Principle of operation



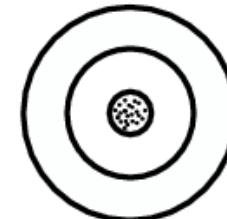
effect	correction (10^{-17})	uncertainty (10^{-17})
BBR room	492.9	1.28
BBR oven	0.94	0.94
second-order Zeeman	3.6	0.15
cold collisions	0	0.08
background gas collisions	0	0.4
line pulling	0	0.01
lattice scalar/tensor	-0.7	0.9
lattice E2/M1	0	0.34
hyperpolarisability	-0.39	0.18
tunnelling	0	0.21
probe light	0	0.01
optical path length error	0	0.01
servo error	0	0.17
DC Stark shift	0	0.03
total	496.4	1.9

Performance of atomic clocks

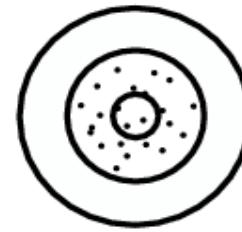
► Systematic uncertainty u_B

- Suppress or control systematic frequency shifts.

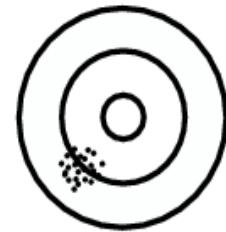
accurate
and stable



accurate
and not stable



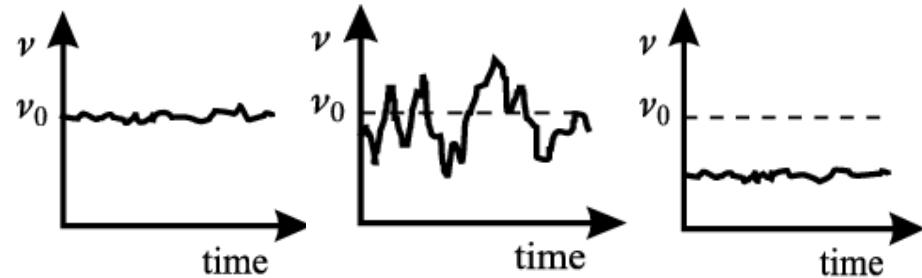
stable, but
not accurate



'precise'

► Instability $\sigma_y(\tau)$

- Expressed by Allan deviation
- $\sigma_y(\tau) \sim \tau^{-1/2}$ for atomic clocks
- Technical and physical limitations



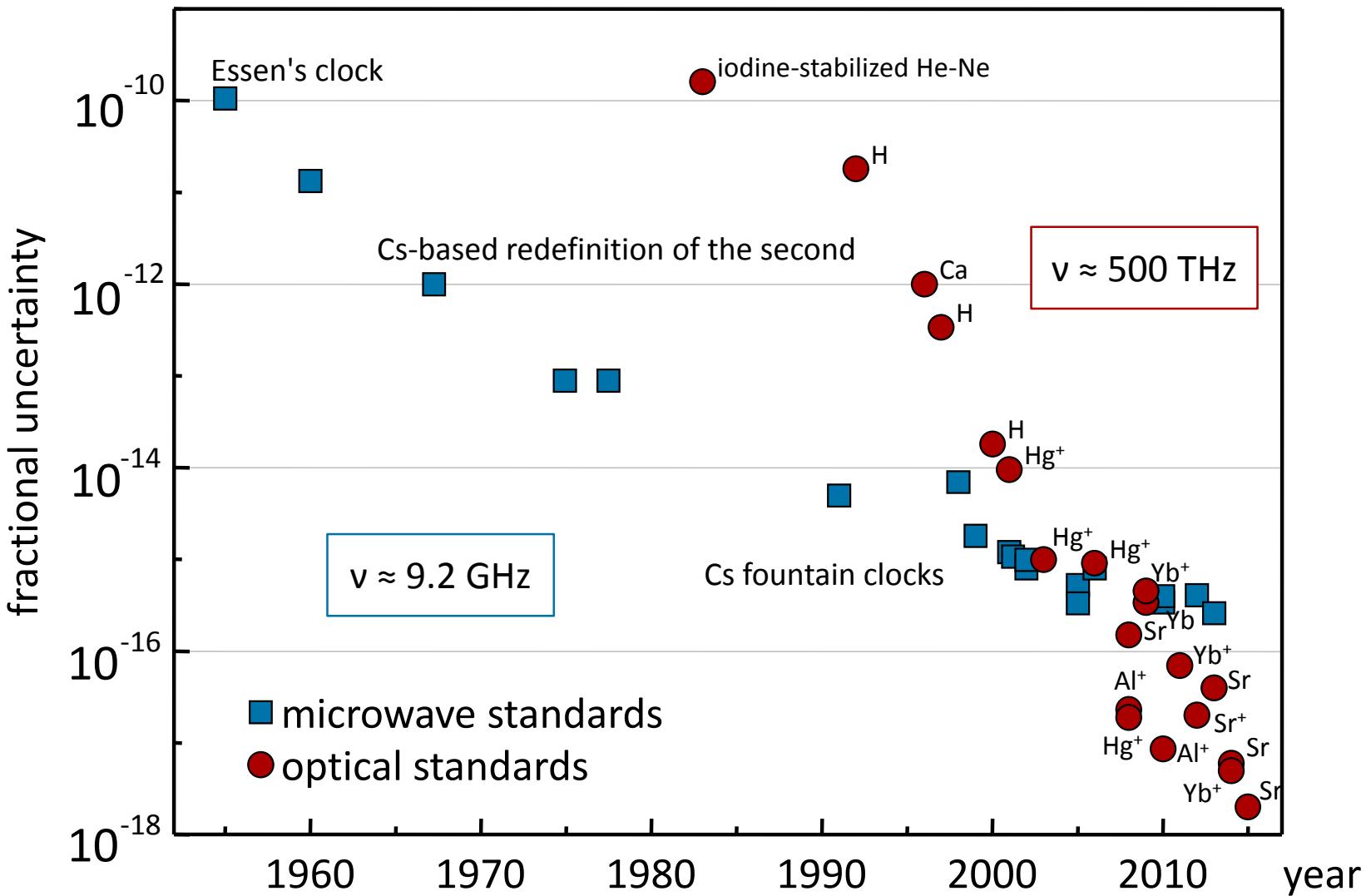
from: F. Riehle, Frequency Standards, Wiley VCH 2004

► Reliability

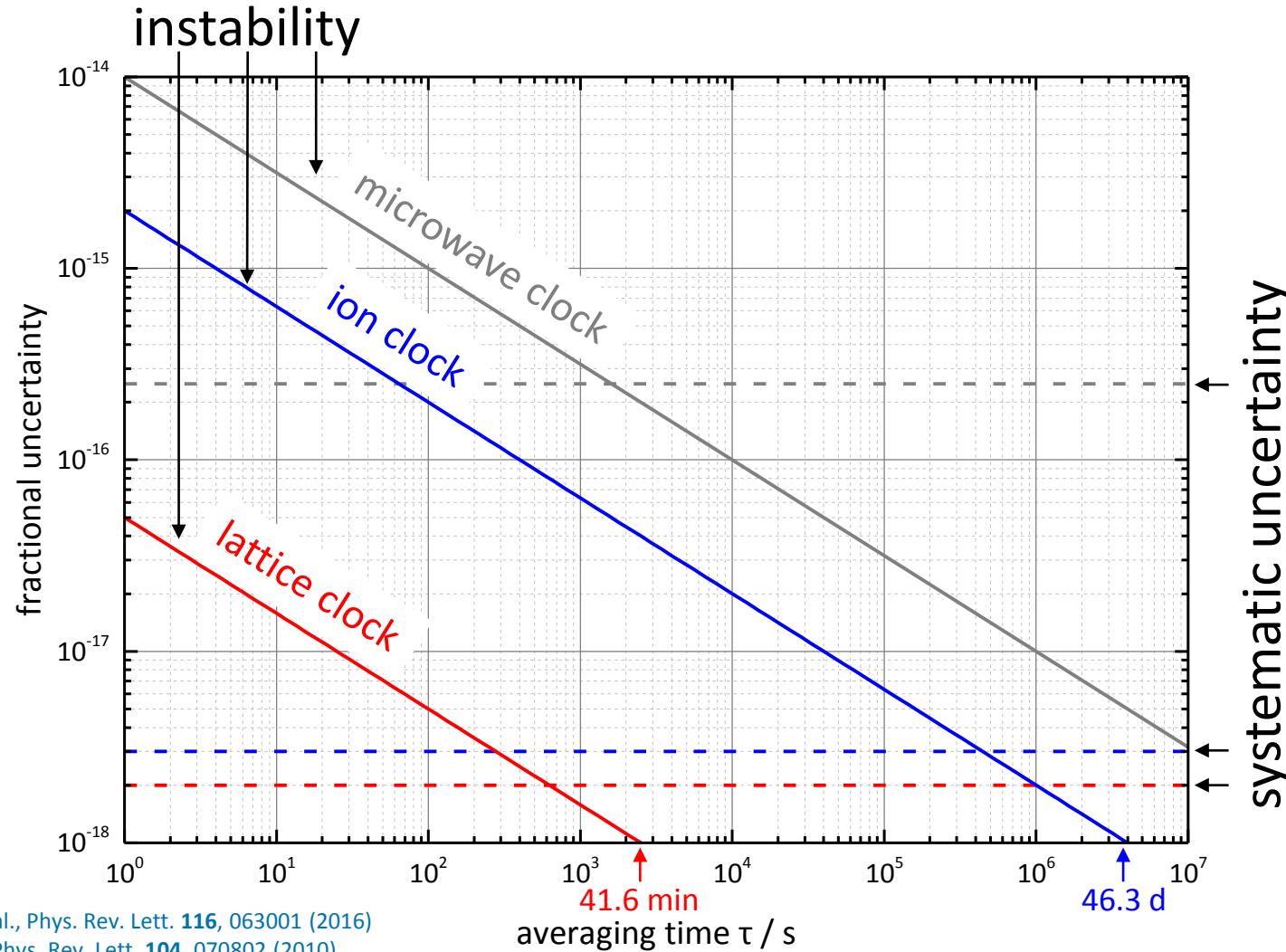
- Minimal interruptions
- Practical long-term operation

Vocabulary in International Metrology (BIPM, IEC, IFCC, ILAC, ISO, IUPAC, IUPAP and OIML)
https://www.bipm.org/utils/common/documents/jcgm/JCGM_200_2012.pdf

Evolution of atomic clocks



Best clock performances



N. Huntemann et al., Phys. Rev. Lett. **116**, 063001 (2016)

C. W. Chou et al., Phys. Rev. Lett. **104**, 070802 (2010)

T. Nicholson et al., Nature Com. **6**, 6896 (2015)

M. Schioppo et al., Nature Photonics **11**, 48 (2017)

Strontium lattice clock

Experimental sequence

200 ms

Zeeman slower
1st stage MOT (461 nm), $T \sim \text{mK}$

90 ms

2nd stage MOT (689 nm)

90 ms

3rd stage MOT (689 nm), $T \sim \mu\text{K}$

65 ms

state preparation
in 1D optical lattice

0.8 s
–
2.6 s

Rabi interrogation (698 nm)
in 1D optical lattice

balanced detection

Partial level diagram

$(5s6s) ^3S_1$

$(5s5p) ^1P_1$

$\lambda = 461 \text{ nm}$

$(\Gamma = 2\pi \times 32 \text{ MHz})$

$\lambda = 689 \text{ nm}$

$(\Gamma = 2\pi \times 7.4 \text{ kHz})$

$J = 2$

1

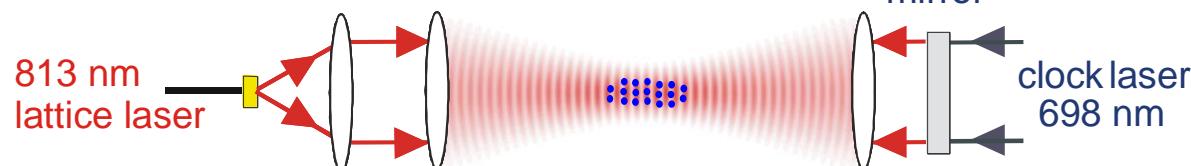
0

$(5s5p) ^3P_J$

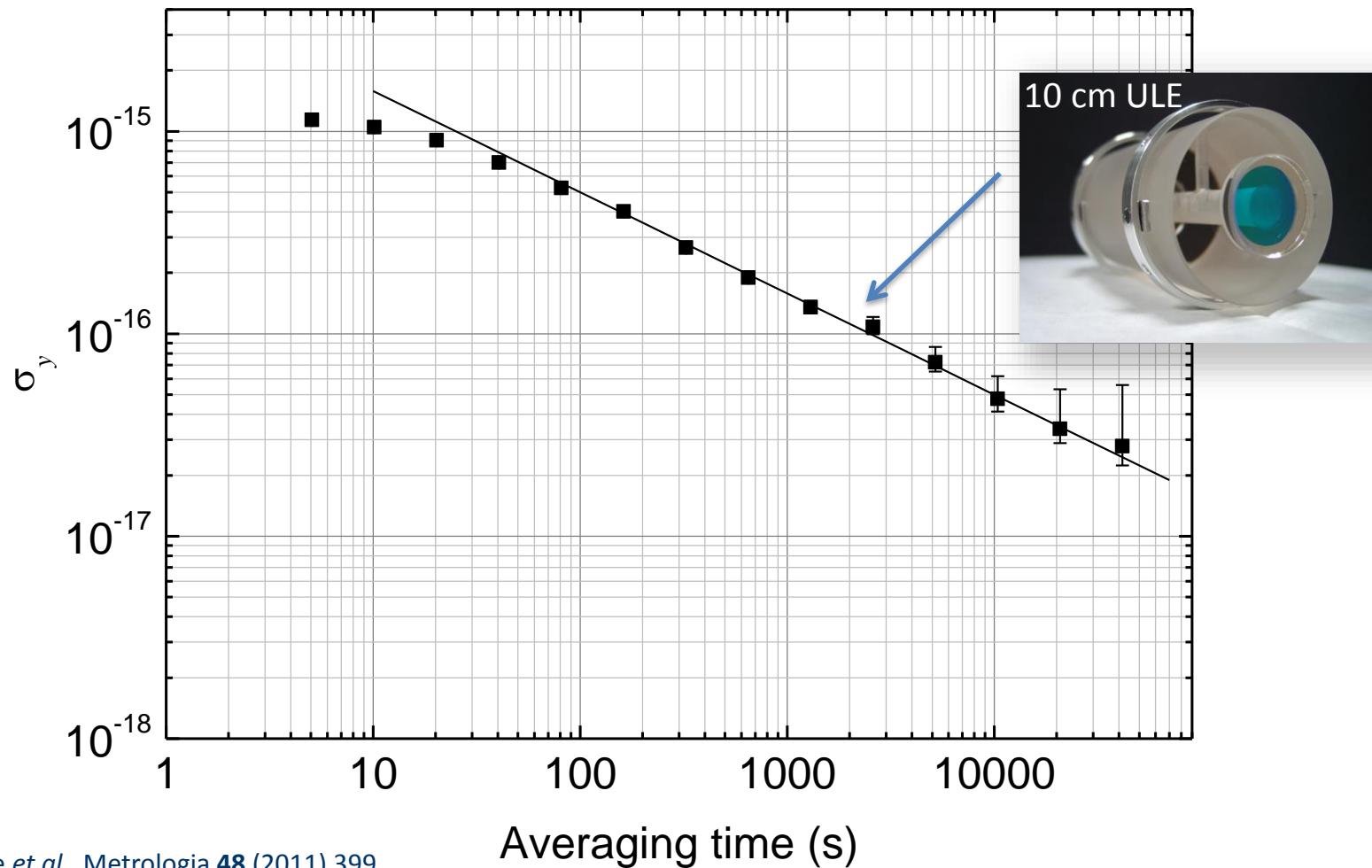
$(5s^2) ^1S_0$

$\lambda = 698 \text{ nm}, v_0 \approx 429 \text{ THz}$
 $(\Gamma \approx 2\pi \times 1 \text{ mHz})$

dichroic
mirror



Importance of the clock laser

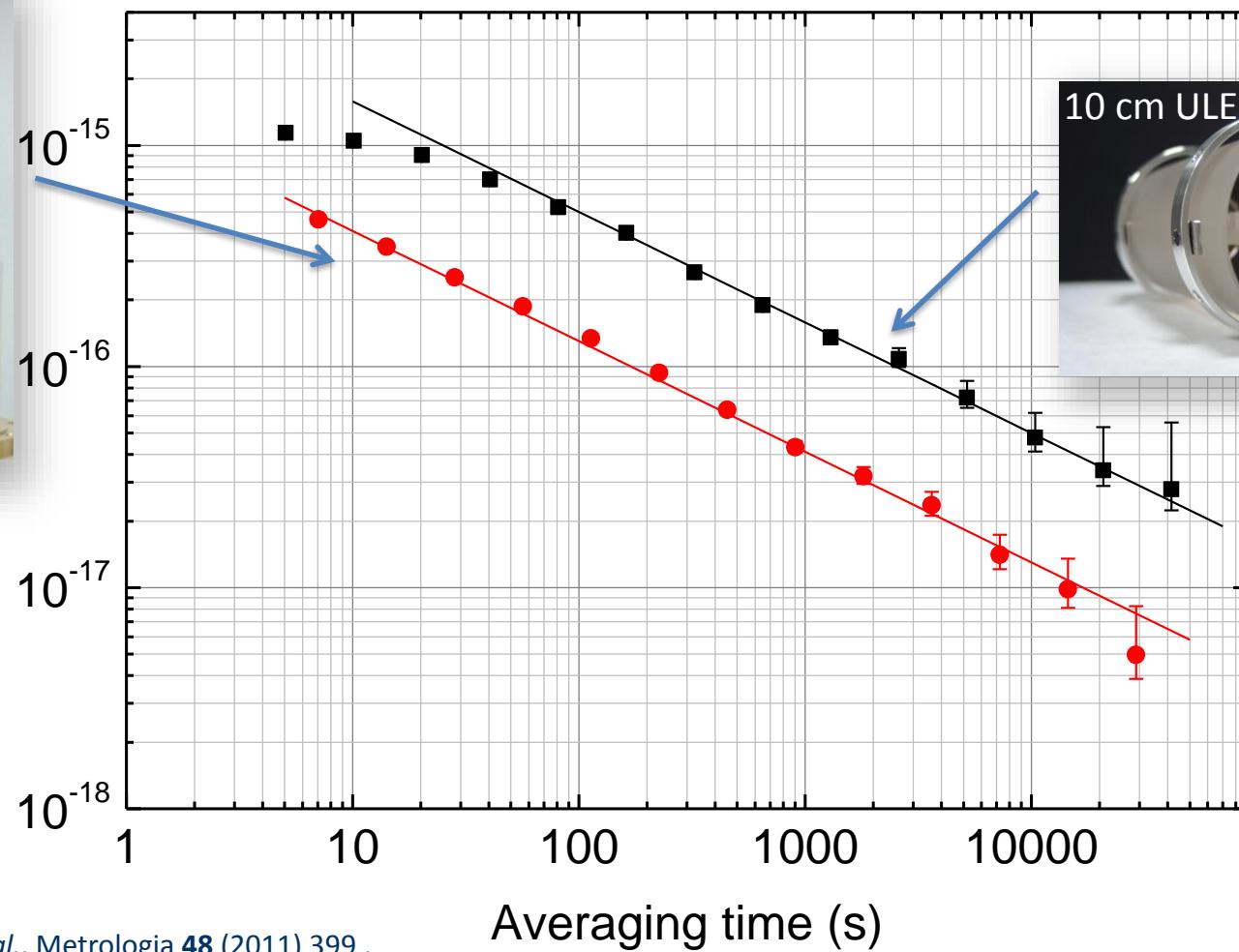


St. Falke *et al.*, Metrologia **48** (2011) 399 ,

Ch. Hagemann *et al.*, IEEE Trans. Instr. Meas. **62** (2013) 1556

A. Al-Masoudi *et al.*, PRA **92**, 063814 (2015)

Importance of the clock laser

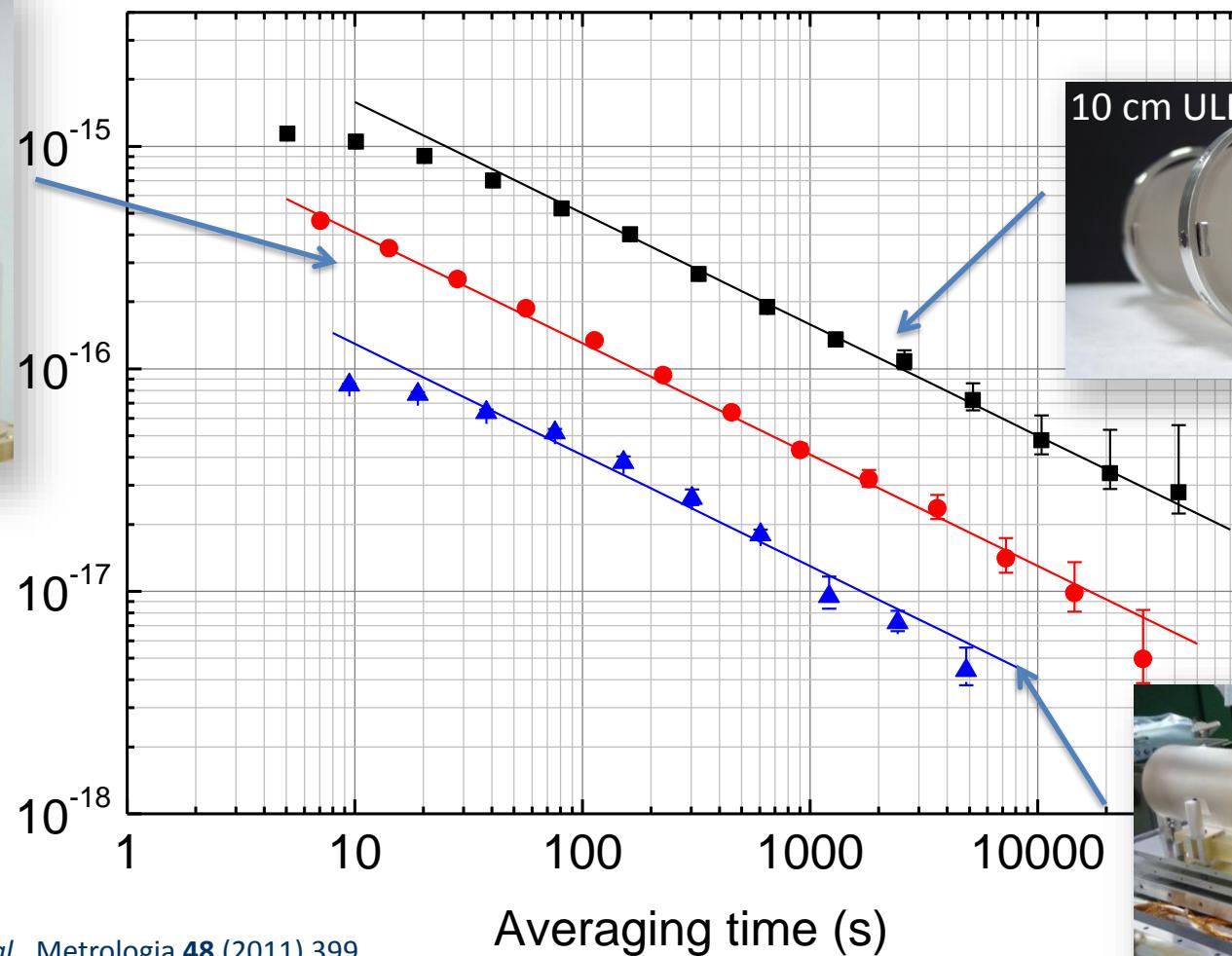


St. Falke *et al.*, Metrologia **48** (2011) 399 ,

Ch. Hagemann *et al.*, IEEE Trans. Instr. Meas. **62** (2013) 1556

A. Al-Masoudi *et al.*, PRA **92**, 063814 (2015)

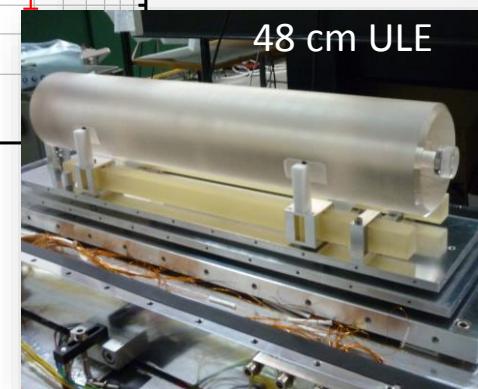
Importance of the clock laser



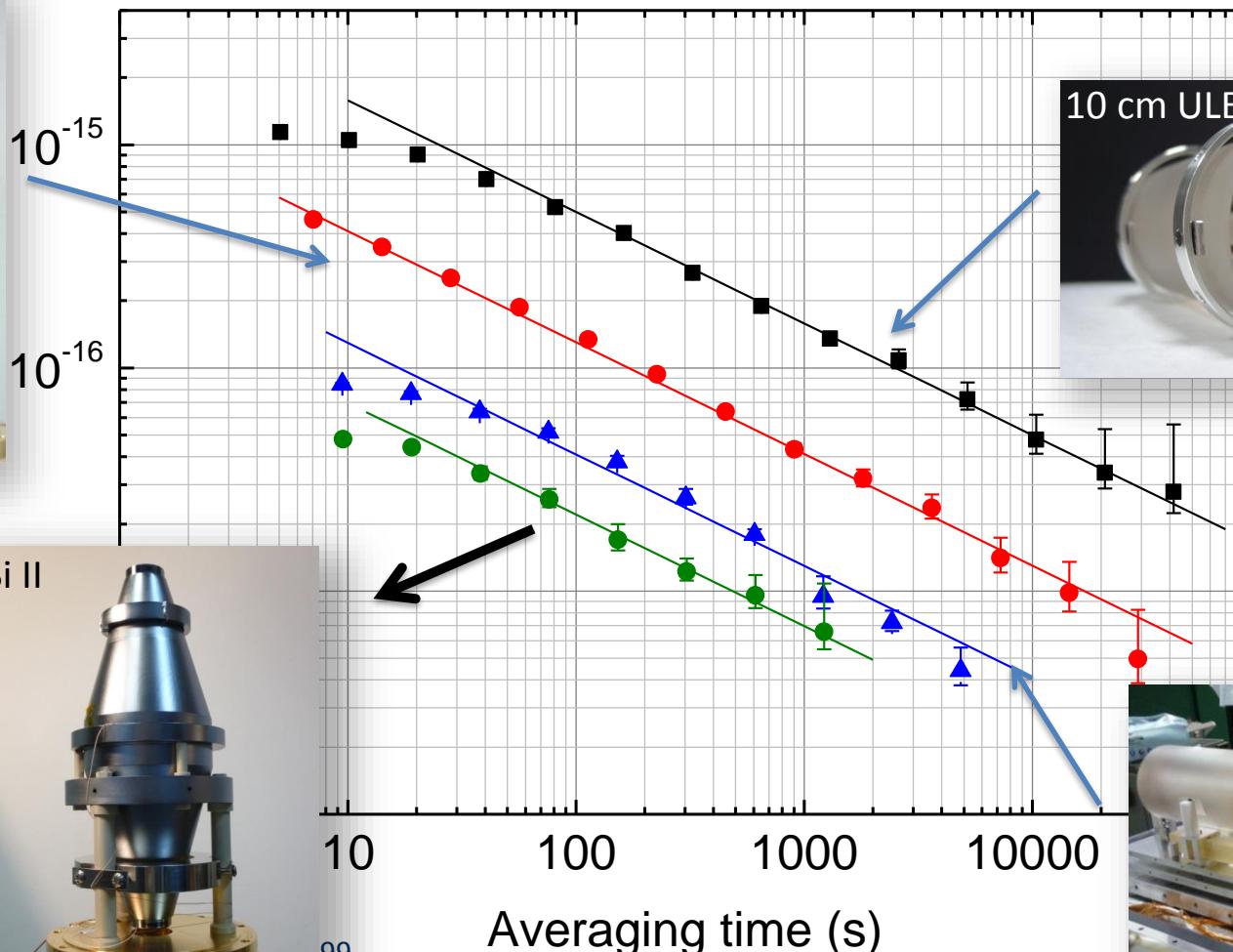
St. Falke *et al.*, Metrologia **48** (2011) 399 ,

Ch. Hagemann *et al.*, IEEE Trans. Instr. Meas. **62** (2013) 1556

A. Al-Masoudi *et al.*, PRA **92**, 063814 (2015)



Importance of the clock laser

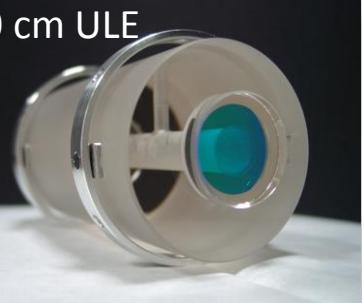


Si II

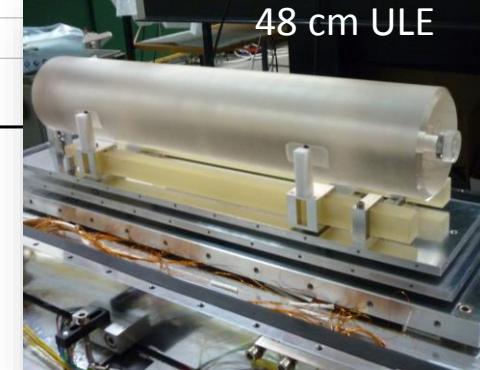


St. Falke e
Ch. Hagen
A. Al-Masoudi *et al.*, PRA 92, 063814 (2015)

99 ,
Meas. 62 (2013) 1556



48 cm ULE



Importance of the clock laser



FEM optimized cavity
shape for minimal
vibration sensitivity

expected thermal noise limit at T = 123.5 K:

$$\text{mod } \sigma_y \approx 4 \times 10^{-17}$$

$$\boxed{\frac{\Delta\nu}{\nu} = -\frac{\Delta L}{L}}$$

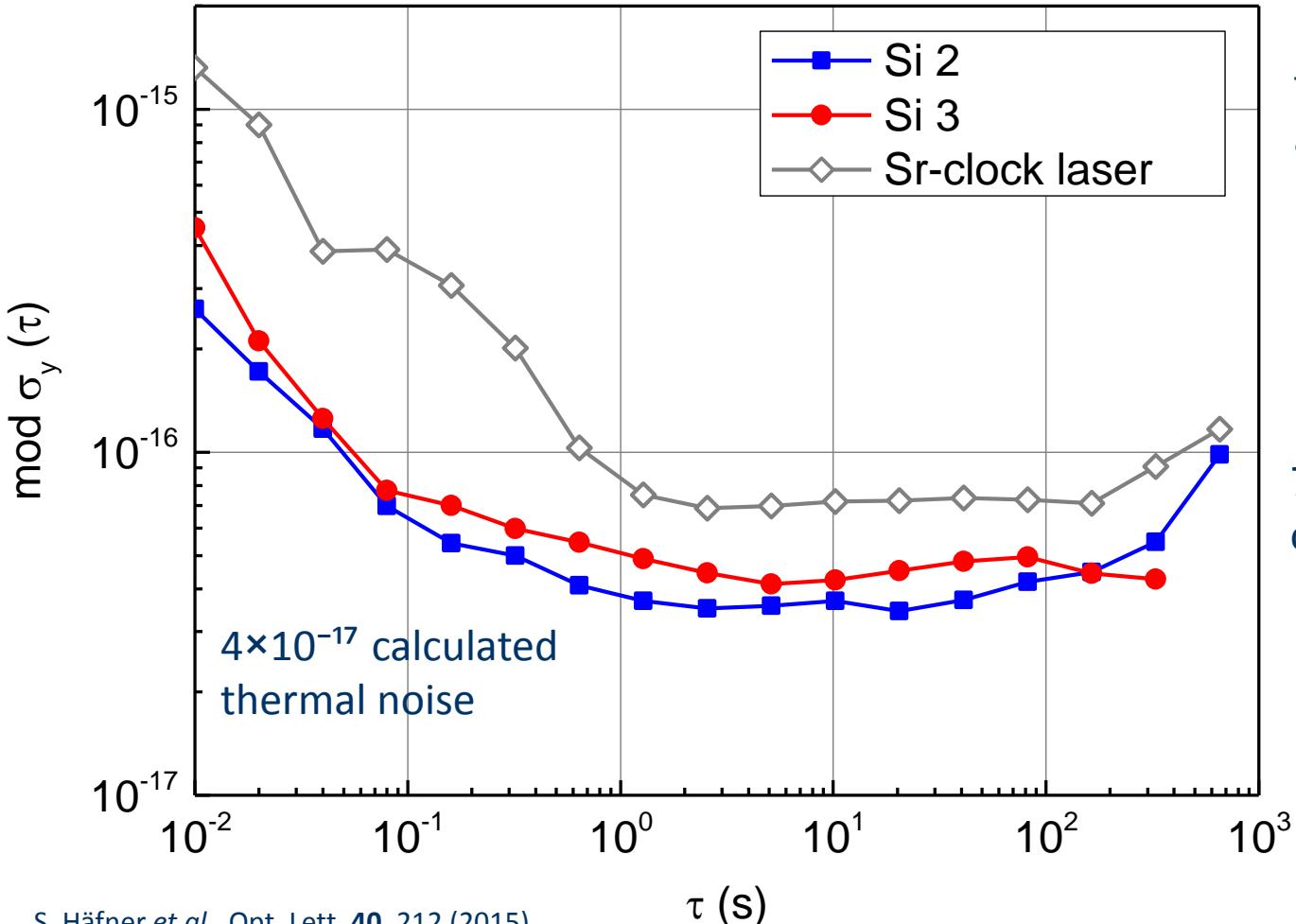
absolute length
fluctuations
 $\approx 8.5 \times 10^{-18} \text{ m}$

dominated by mirror coatings!

T. Kessler *et al.*, Nature Phot. 6, 687 (2012),
D. Matei *et al.*, Phys. Rev. Lett. 118, 263202 (2017)

proton diameter $\approx 0.85 \text{ fm} = 850 \times 10^{-18} \text{ m}$

Importance of the clock laser



linear drift removed
from Si 3 – Si 2
and Sr – Si 2 beats

7×10^{-17} thermal noise
of ULE cavity

S. Häfner *et al.*, Opt. Lett. **40**, 212 (2015),
 T. Kessler *et al.*, Nature Phot. **6**, 687 (2012),
 D. Matei *et al.*, Phys. Rev. Lett. **118**, 263202 (2017)

What can you do?



Yb⁺ single
ion clock



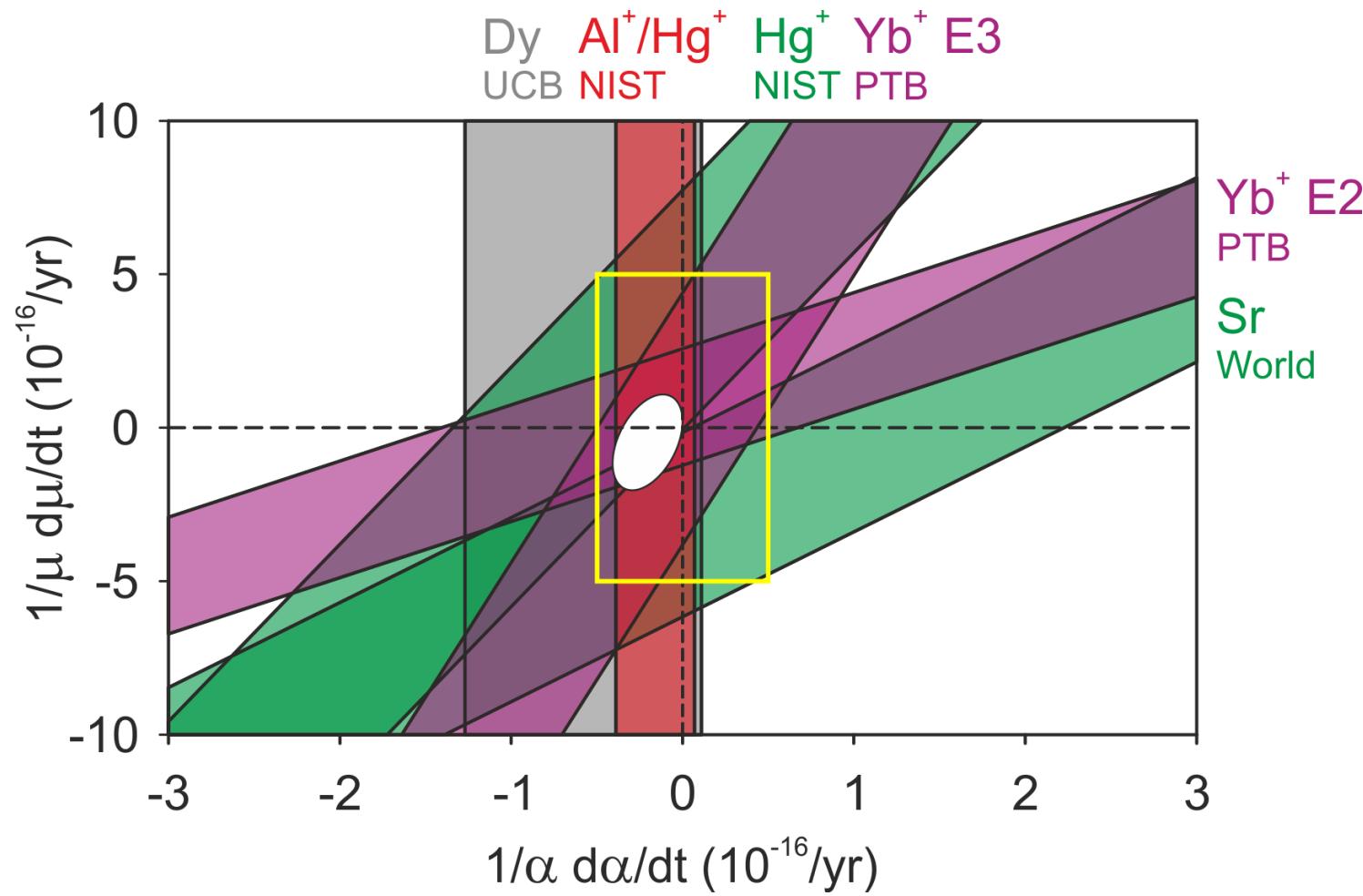
building A

building B



Sr lattice
clock

Repeated comparisons – interpretation

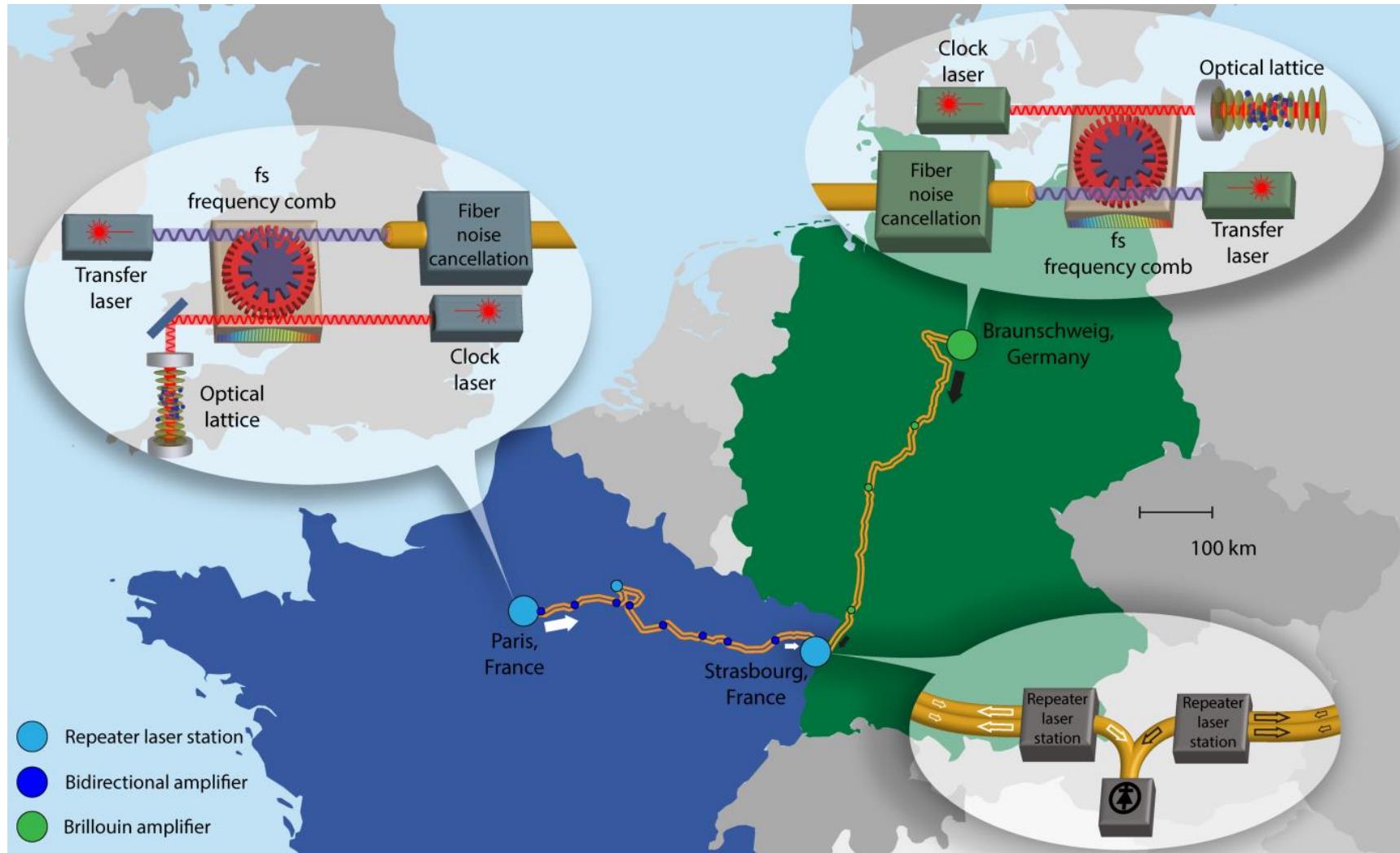


N. Huntemann *et al.*, Phys. Rev. Lett. **113**, 210802 (2014)

R. Godun *et al.*, Phys. Rev. Lett. **113**, 210801 (2014)

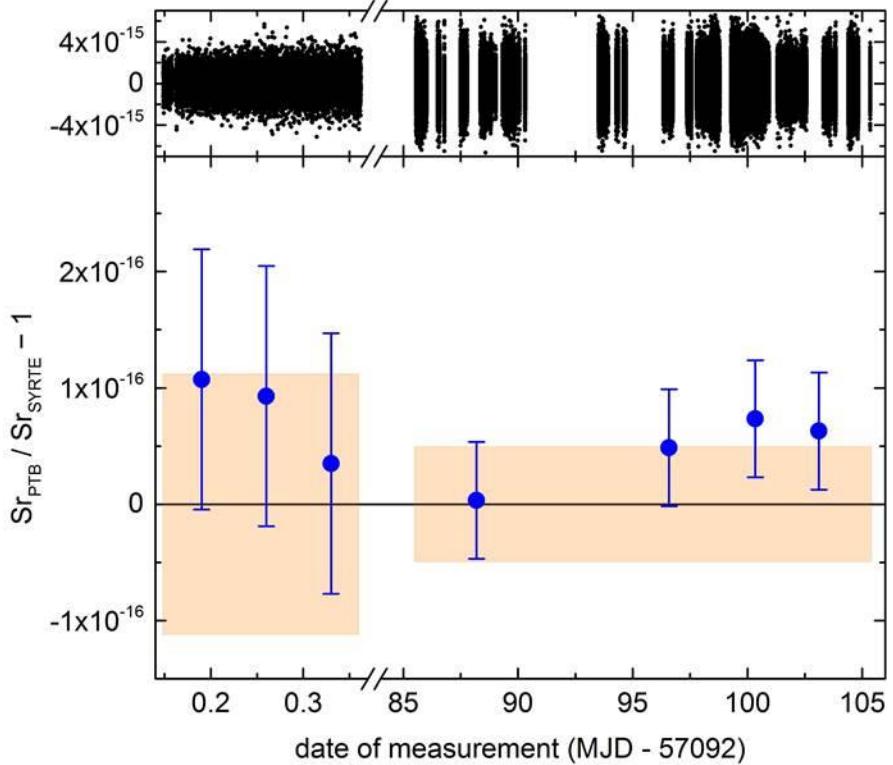
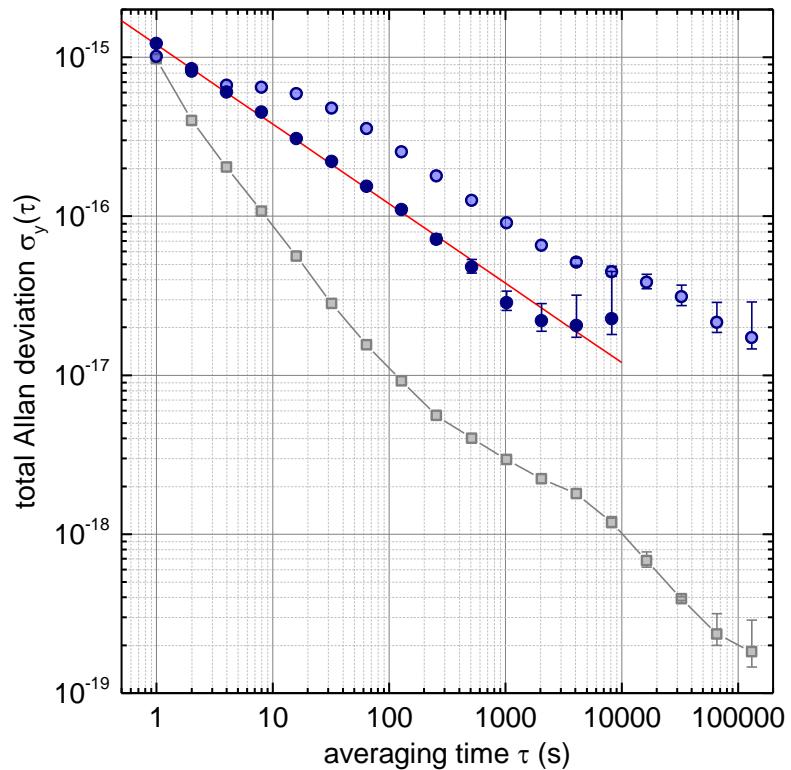
T. Rosenband *et al.*, Science **319**, 1808 (2008)

Clock comparisons – local and non-local



Ch. Lisdat *et al.*, Nature Comms. 7, 12443 (2016)

Clock comparisons – Paris & Braunschweig



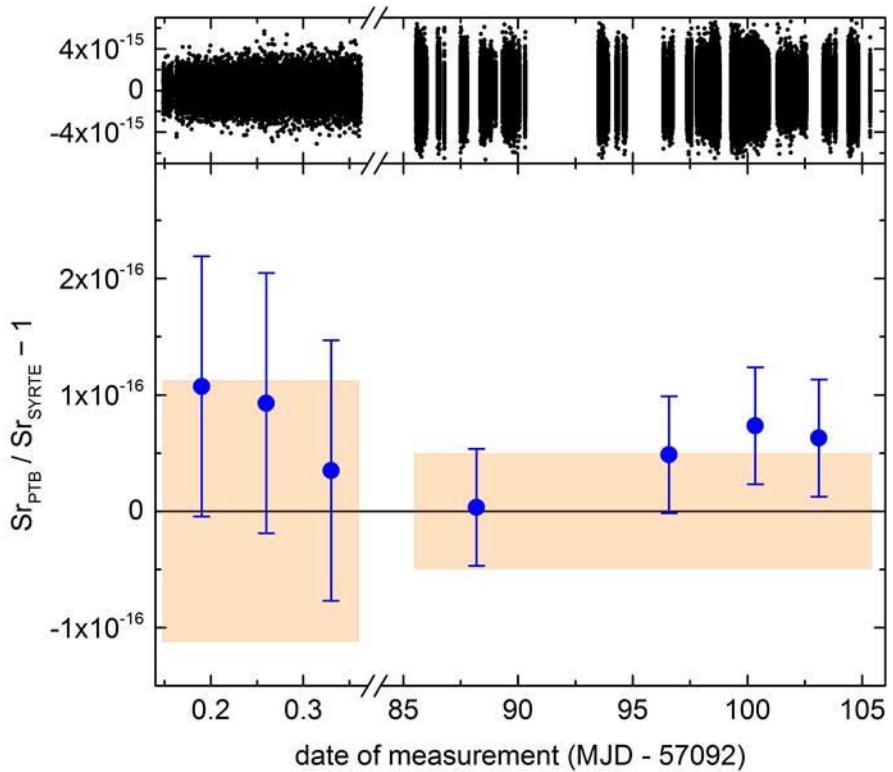
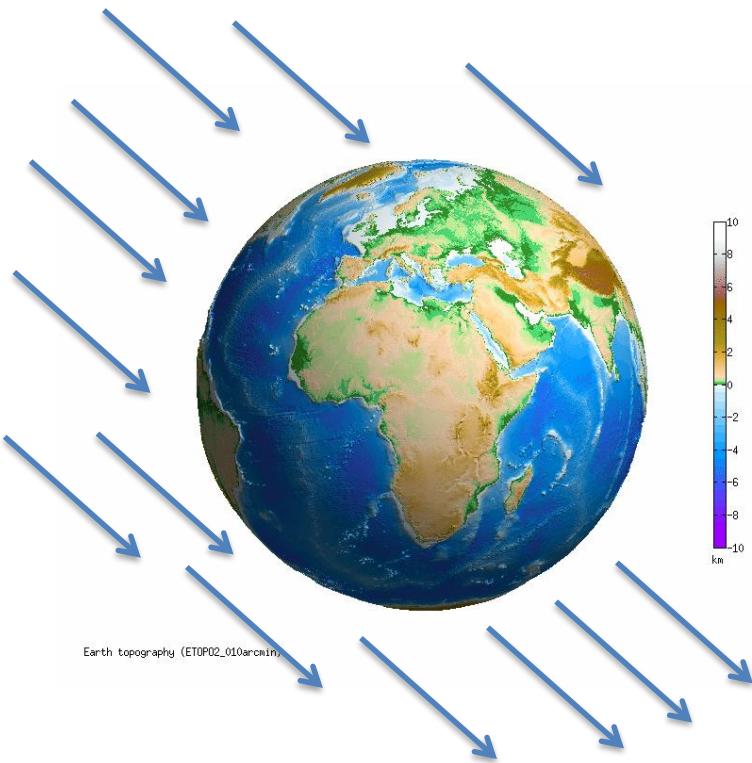
Gravity potential correction
 $-247.2(4) \times 10^{-17}$



Ch. Lisdat *et al.*, Nature Comms. 7, 12443 (2016)

Clock comparisons – Paris & Braunschweig

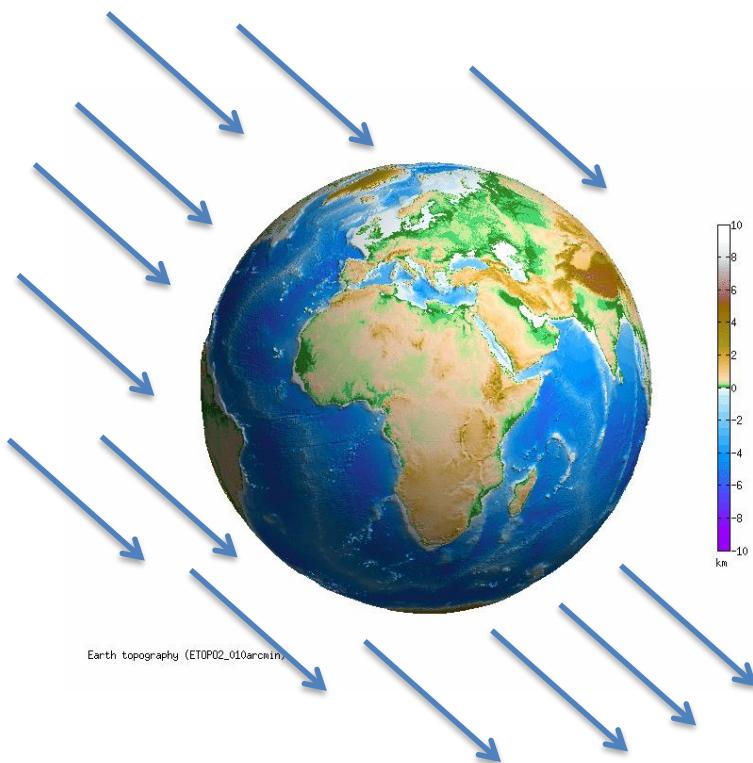
Local Lorentz invariance: search for daily modulation due to motion wrt. background



animation: A. Bezdek and J. Sebera, Computers & Geosciences 56, 127 (2013), data set: ETOPO2 / EGM2008

Clock comparisons – Paris & Braunschweig

Local Lorentz invariance: search for daily modulation due to motion wrt. background



was done with Rb clocks (GPS)
P. Wolf & G. Petit, Phys. Rev. A **56**, 4405 (1997)

$$|\alpha| \leq 10^{-6}$$

LLI test also with fast ion beams
B. Botermann *et al.*, Phys. Rev. Lett. **113**, 120405 (2014)

$$|\alpha| \leq 2 \times 10^{-8}$$

Sr clocks London, Paris, Braunschweig
P. Delva *et al.*, Phys. Rev. Lett. **118**, 221102 (2017)

$$|\alpha| \leq 1.2 \times 10^{-8}$$

animation: A. Bezdek and J. Sebera, Computers & Geosciences **56**, 127 (2013), data set: ETOPO2 / EGM2008

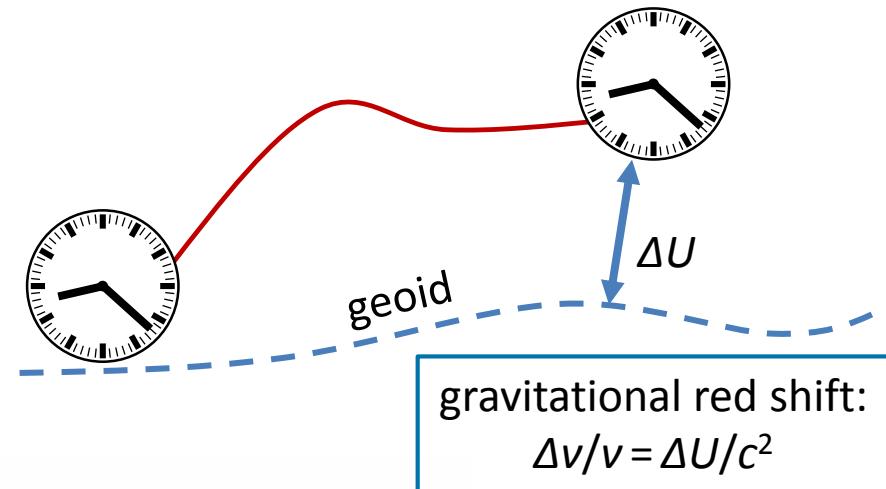
Leaving the lab: Transportable clocks

- ▶ flexibility of clock pairs
- ▶ choose operation sites
to probe the gravity potential
- ▶ first step towards space

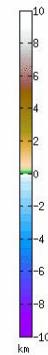
Transportable optical clocks

► Optical clocks as sensors:

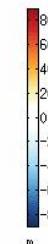
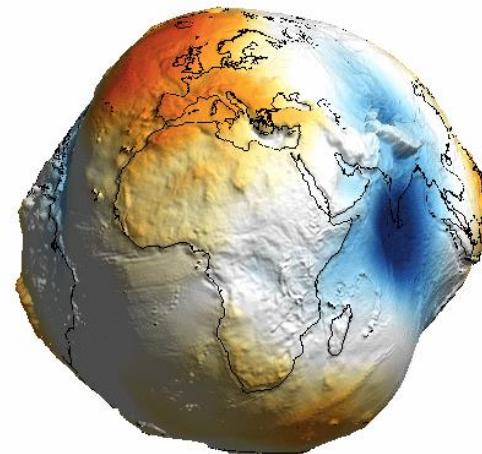
- Directly measure potential differences.
- Vision: Realize geoid by clocks.



Earth topography (ETOPO2_010arcmin)



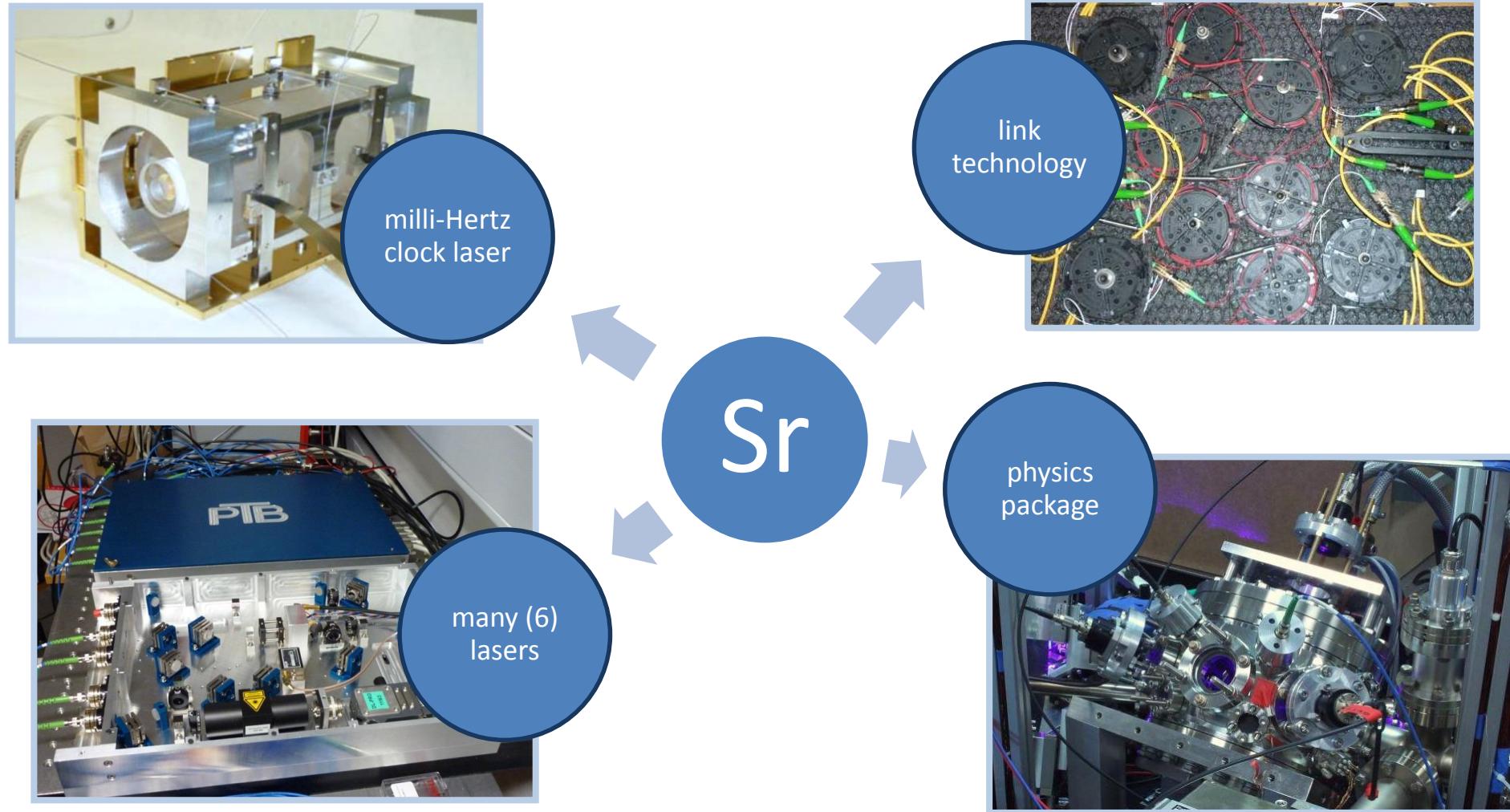
Geoid height (EGM2008, nmax=500)



M. Vermeer, Rep. of the Finnish Geod. Insti. **83**, 1 (1983)

A. Bjerhammar, Bull. Geodesique **59**, 207 (1985)

Transportable optical clocks



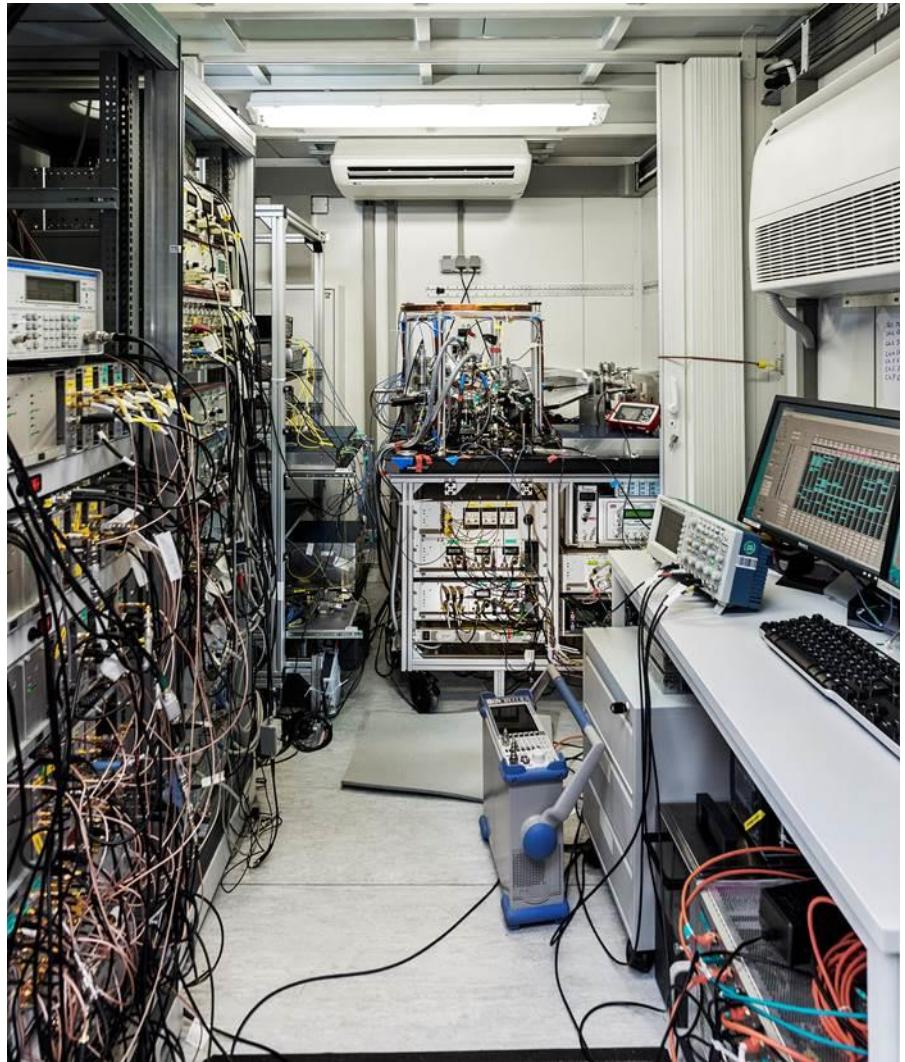
Transportable optical clocks



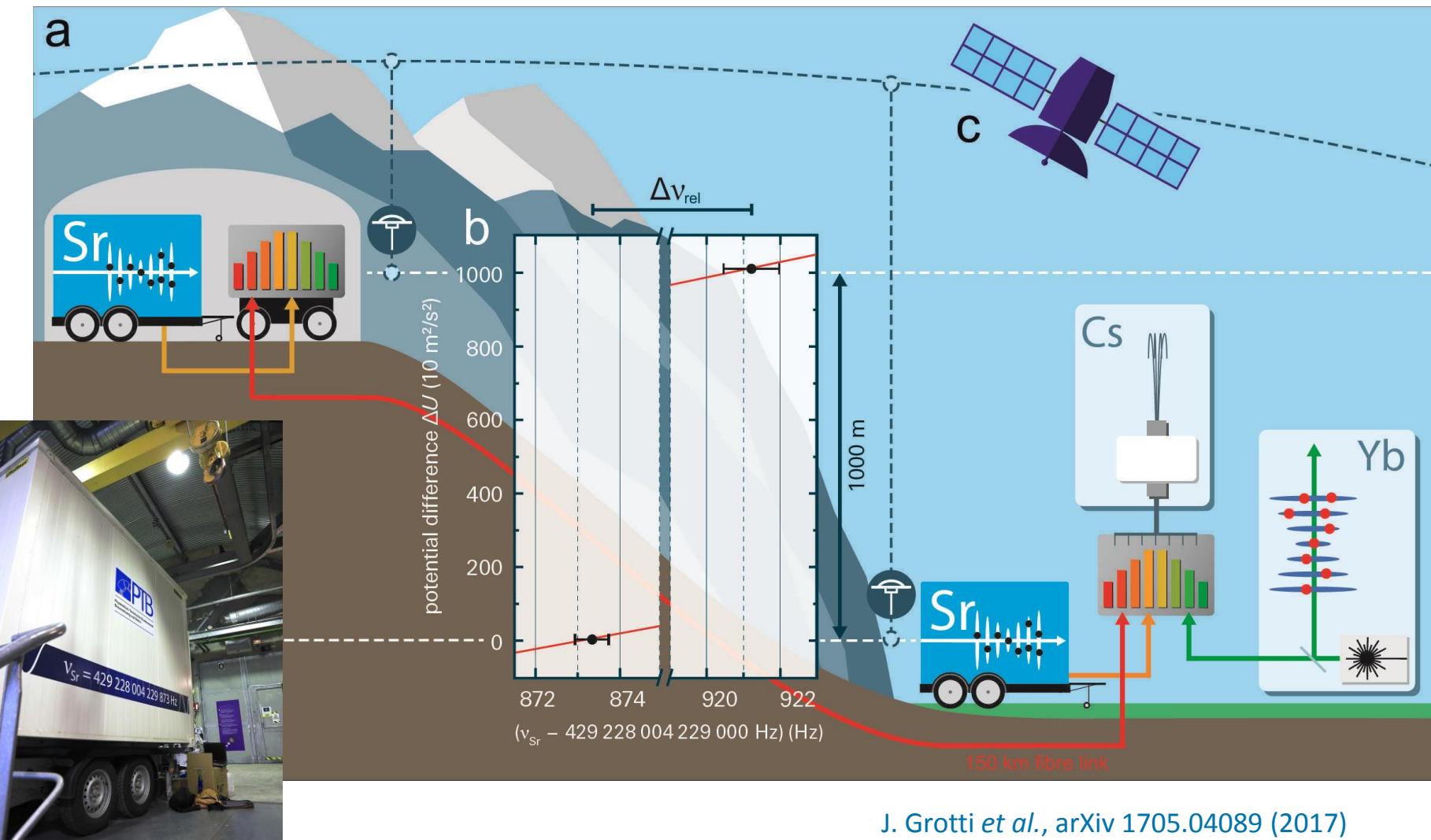
Car trailer housing the clock

S. Koller *et al.*, Phys. Rev. Lett. **118**, 073601 (2017)

View into the car trailer ➤

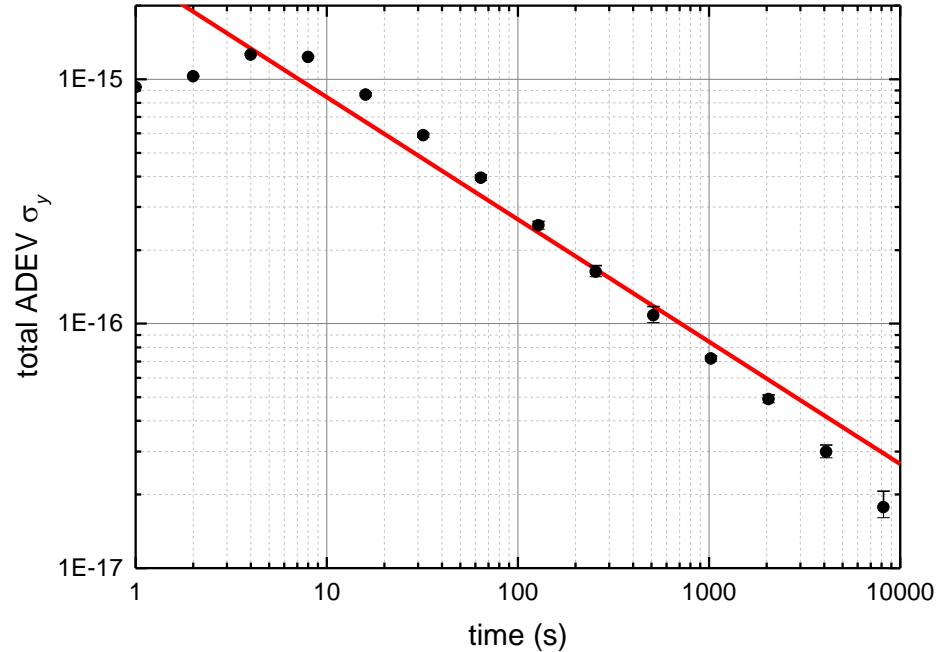


First time off-campus: Modane – Torino 2016



J. Grotti *et al.*, arXiv 1705.04089 (2017)

Second campaign: Paris – Braunschweig 2017



Combined uncertainty $\approx 3 \times 10^{-17}$ or 30 cm in 3 hours.

Gravity potential correction from geodesy: $-247.2(4) \times 10^{-17}$

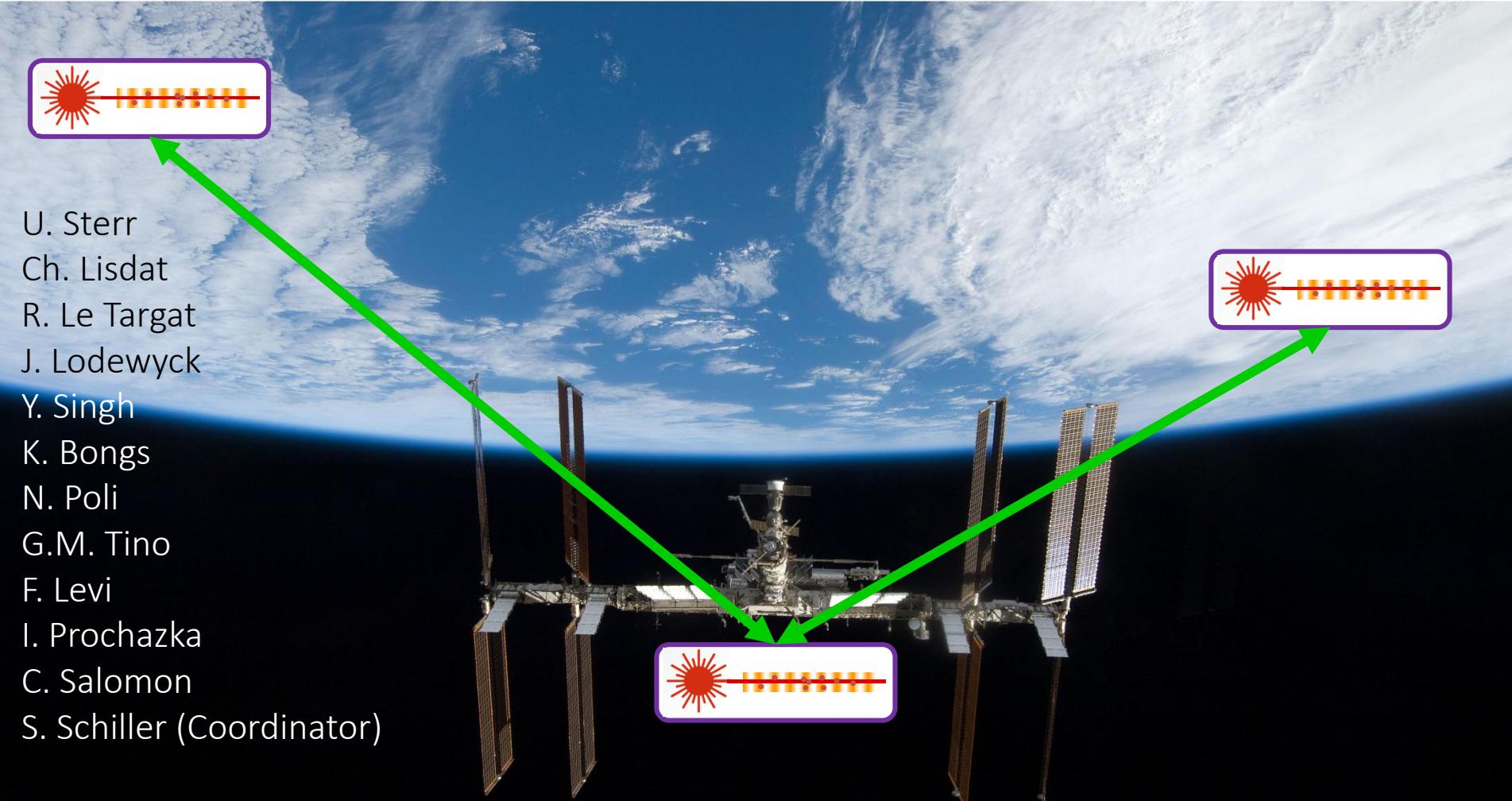
unfortunately: ‘anomaly’ in the second half of the campaign

Status PTB's transportable lattice clock

- ▶ Approaching design uncertainty of 1×10^{-17}
- ▶ Reliability is still a problem
 - but it is obvious that you can do better
- ▶ Balance design/construction effort with salary of PhD student
- ▶ Next generation:
 - lower uncertainty ($1 \times 10^{-18}?$)
 - more ‘user friendly’
 - as heavy and power hungry



Mission I-SOC: An optical clock on the ISS



Science goals of I-SOC

Explore the limits of our physical laws:

- Test Einstein's prediction of time dilation (*Earth, Sun, Moon*)
- Test of the gravitational-potential independence of fundamental constants
- Kennedy-Thorndike experiment
- Support search for dark matter topological defects

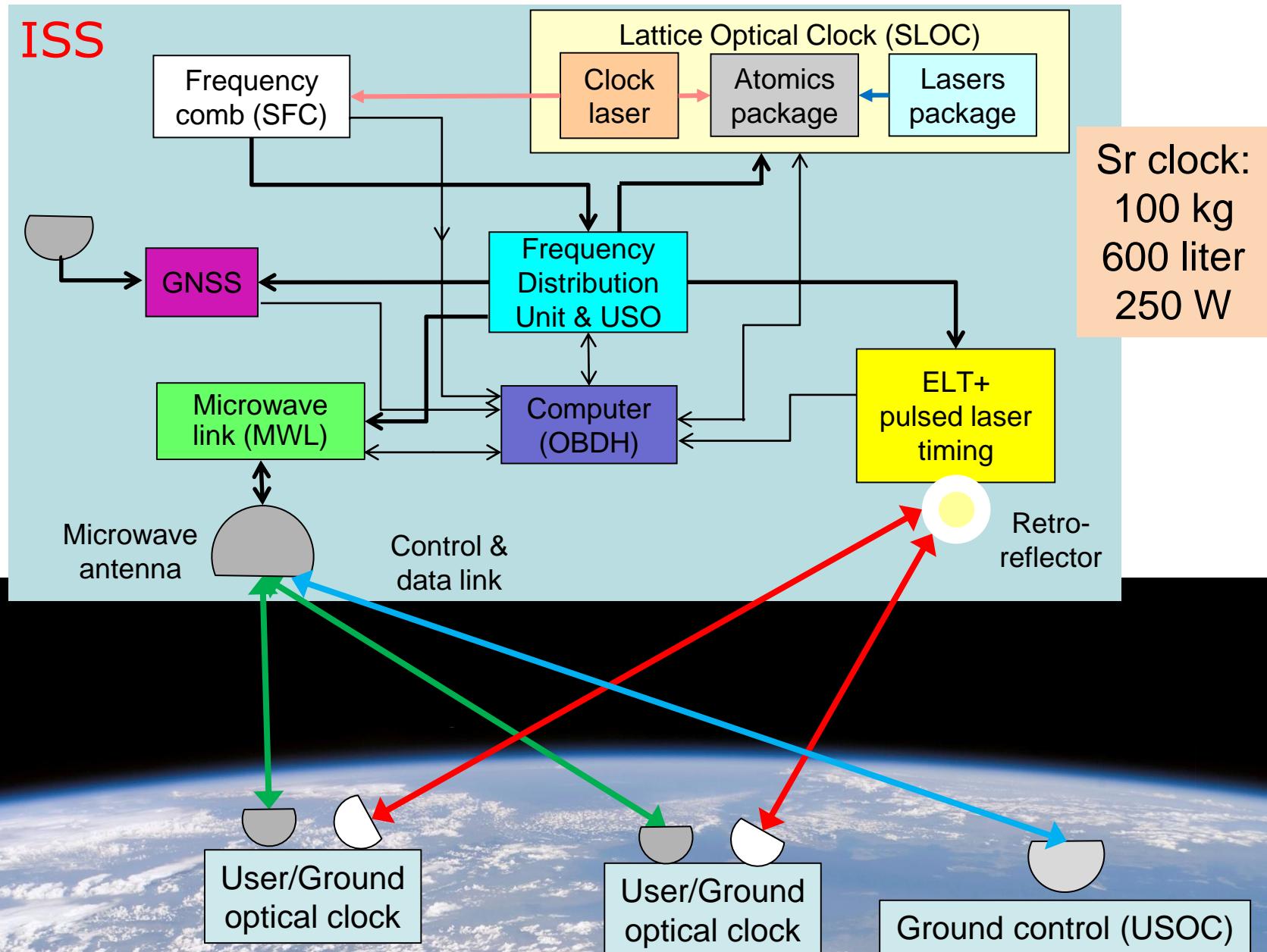
Frequency links + high-performance clock in space:

- Timekeeping: comparison of distant terrestrial clocks
- Relativistic geodesy: determination of the local gravity potential at 1 cm equivalent level within 1 day measurement time

Master clock in space:

- Delivery of atomic time to ground and (optionally) to spacecrafts

I-SOC payload: concept



ACES and I-SOC

- ACES actual/estimated performance vs. I-SOC requirements

	ACES	I-SOC *	Improvem.
Clock instability	$1 \times 10^{-13} / \tau^{1/2}$	$8 \times 10^{-16} / \tau^{1/2}$ (τ up to 2×10^6 s)	x 100
Clock uncertainty	1×10^{-16}	1×10^{-17}	x 10
MWL / MWL+ TDEV	$1.5 \text{ ps} \times (\tau / 10,000 \text{ s})^{1/2}$	0.03 ps ** $\tau > 1000$ s	x 150 @ 1 day
ELT / ELT+ TDEV	8 ps @ 10^6 s	1 ps @ 10^6 s	x 8
Phase coherence	yes	yes, minimum 12 h up to 10 days (25 times)	

- I-SOC clock signal shall be phase-coherent → requirement to comb and SLOC
- ELT+ supports reaching 1×10^{-18} ground clock comparisons (or ground-space)
- I-SOC performance can be tested fully on the ground (*trapped atoms*)

* from I-SOC ESR document

** ground-to-space

I-SOC: way forward

New approach by ESA:

Science team is strongly involved in all phases of mission development

1) ESA technology developments

- *462 nm, 689 nm lasers*
- *CCU: laser frequency stabilization system*
- *813 nm lattice laser*
- *Clock laser reference cavity (1397 nm)*
- *Two-way microwave link*

2016-2018:

[Fraunhofer UK, TopGaN,CNR,**HHU**]
[NPL UK, **PTB**]
[Fraunhofer UK, **SYRTE**]
[Airbus F'hafen, NPL, SpaceTech, **PTB**]
[Timetech, DLR Oberpf., **SYRTE**]

2) Experiment Science Document

2/2017 [**Science team**]

3) Phase-A study, scientific part

2017 [**Science team**]

4) Phase-A study, industrial part

2018 [*space industry*, **Science team**]

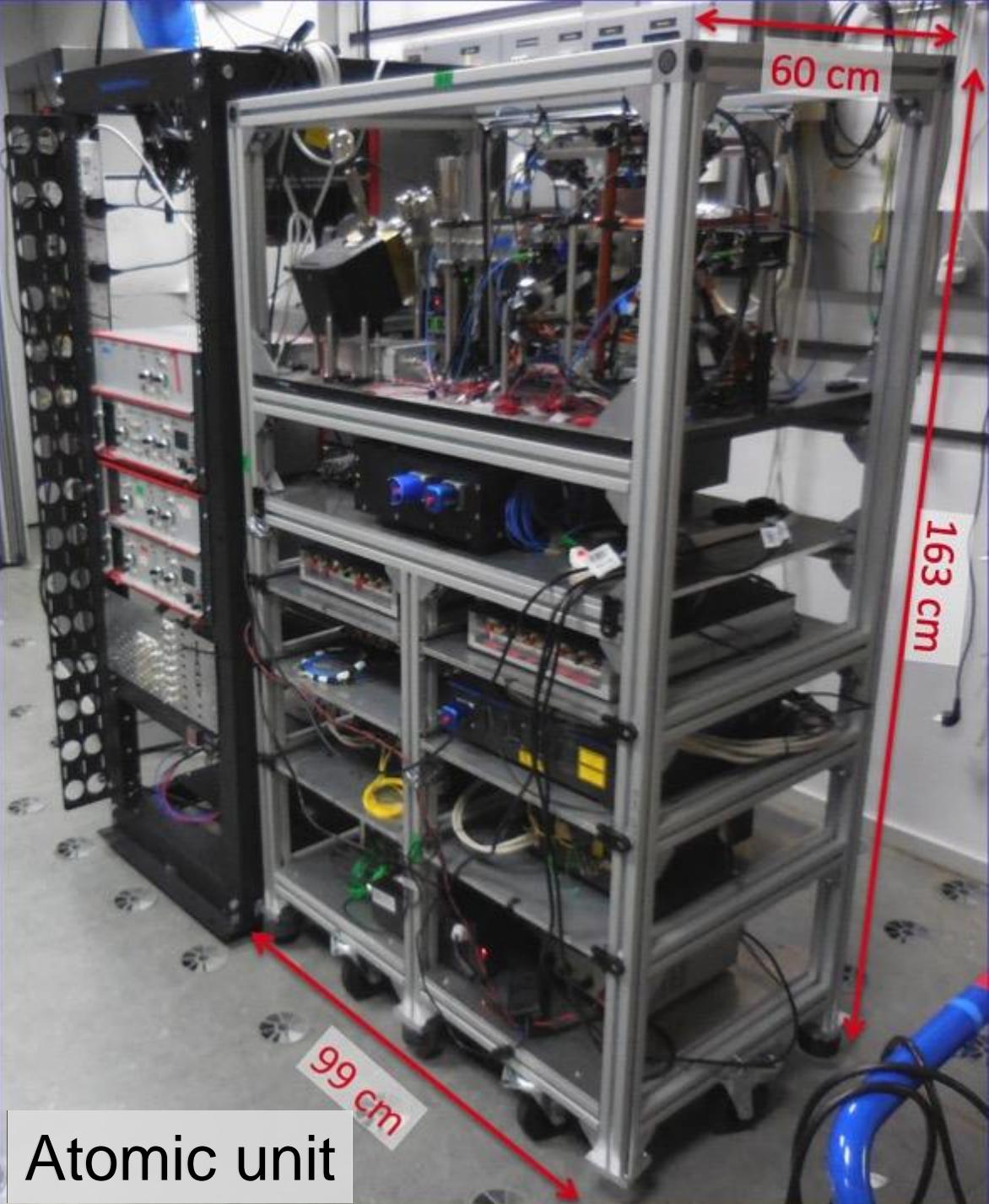
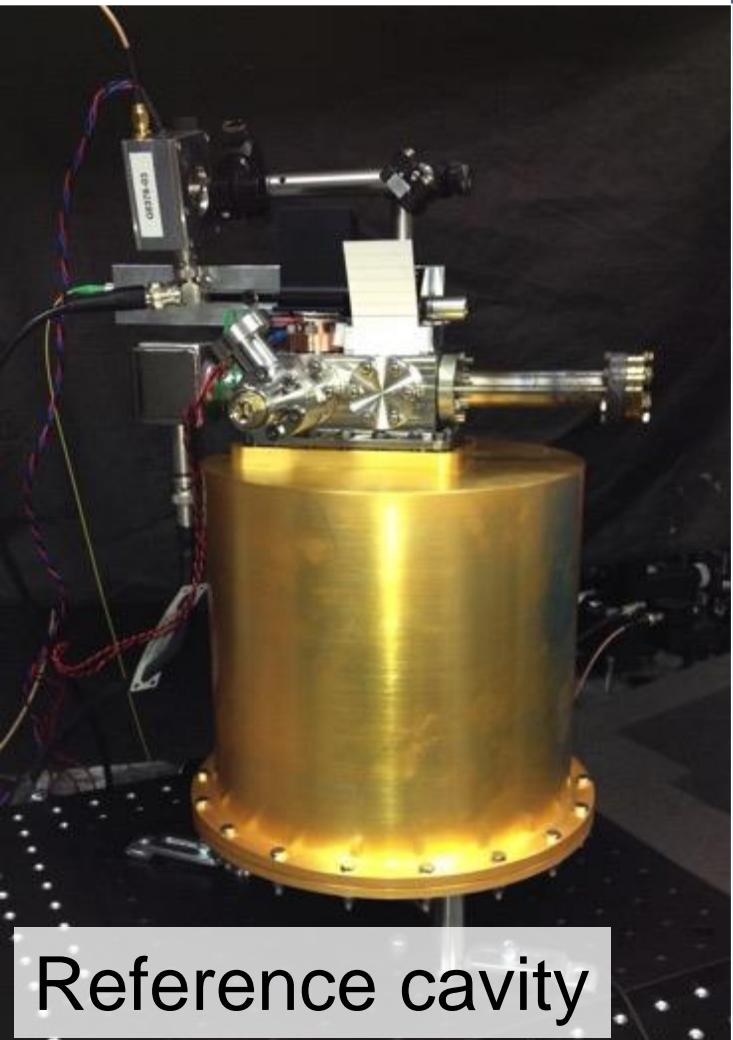
5) Phases B, C

2019+ [*space industry*, **Science team**]

Mission

2022+

I-SOC: Sr lattice clock demonstrator



I-SOC: Sr lattice clock demonstrator



References:

SOC project:

S. Schiller *et al.*, "Let's embrace space" Vol. II, Ch. 45, 452
(Luxembourg: Publications Office of the European Union, 2012)

Sr breadboard:

Origlia, S. et al., Proc. SPIE Photonics Europe 2016, arXiv:1603.06062
K. Bongs, *et al.*, C. R. Phys. **16**, 553 (2015)

Clock laser:

D. Świerad *et al.*, Sci. Rep. **6**, 33973 (2016).

Zeeman slower:

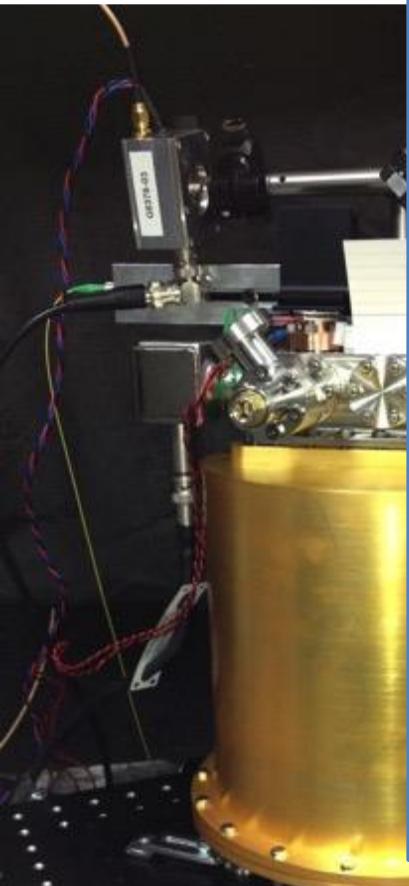
I.R. Hill *et al.*, J. Phys. B. **47**, 075006 (2014)

Atomic oven:

M. Schioppo, *et al.*, Rev. Sci. Instrum. **83**, 103101 (2012)

Frequency stab. system:

A. Nevsky *et al.*, Opt. Lett. **38**, 4903 (2013)



Reference cavity



Atomic unit

^{88}Sr (boson) vs. ^{87}Sr (fermion)

^{88}Sr

Isotopic abundance: 83%

Laser cooling easier

Shorter cycle time (2 interrogations)

Insensitive to vector and tensor light shift

Need for magnetically induced spectroscopy:

- 1) Large magnetic field
- 2) Large clock laser beam intensity

s-wave collisions

May have advantages in terms of simplicity and for transportability

^{87}Sr

Isotopic abundance: 7%

Nuclear spin ($I = 9/2$): laser cooling more complicated (1 more laser)

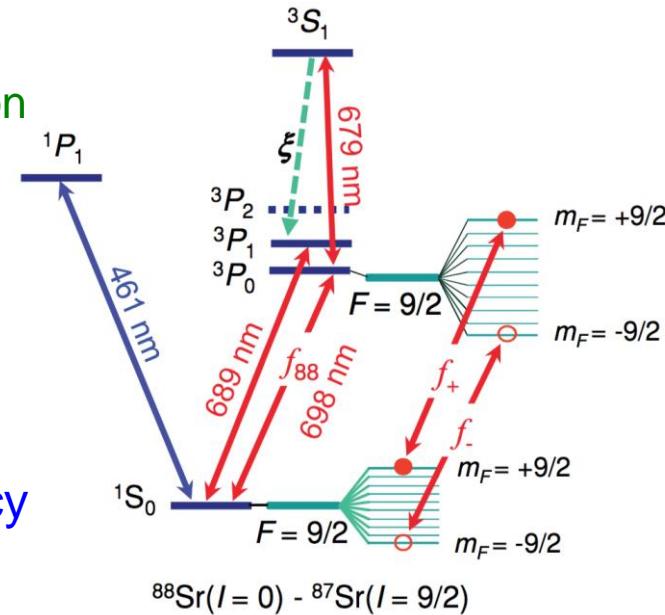
1st order Zeeman shift (4 interrogations)

Sensitive to vector and tensor light shift

Hyperfine interaction allows $^1\text{S}_0$ - $^3\text{P}_0$ transition

Only p-wave collisions

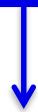
Better for accuracy



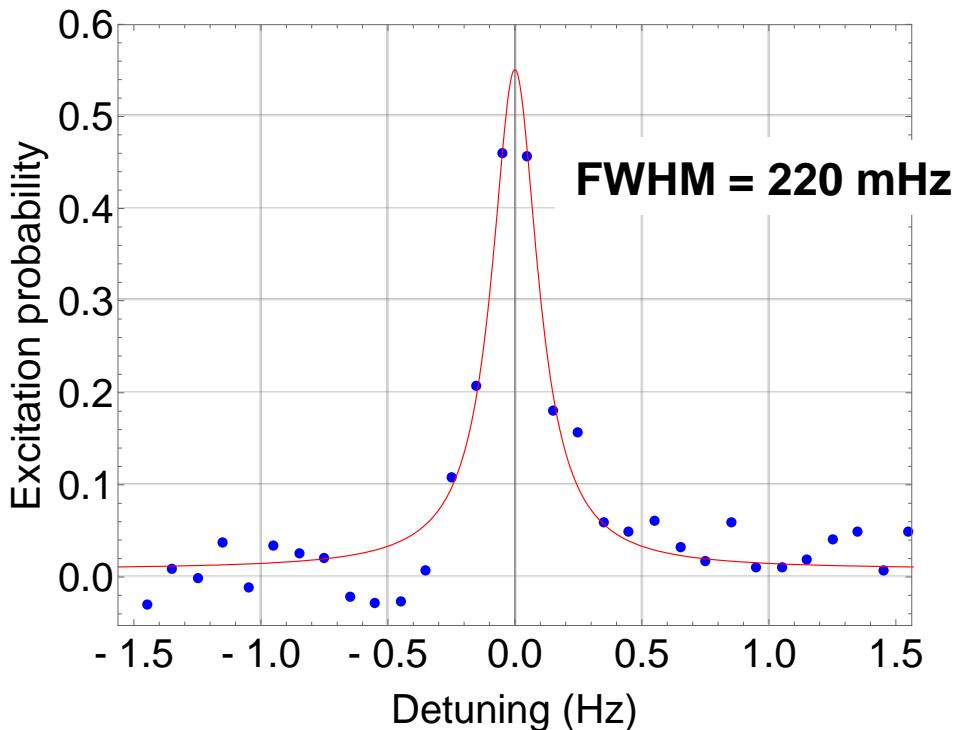
I-SOC Clock transition line in ^{88}Sr (698 nm)

Long interrogation time:
4 s (Fourier-limited linewidth)

$$\begin{aligned} |B| &= 0.20 \text{ mT} & Dn_B &\approx 0.9 \text{ Hz} \\ I &= 14 \text{ mW/cm}^2 & Dn_I &\approx 0.5 \text{ Hz} \end{aligned}$$



For $<10^{-17}$ relative stability,
 I and B have to be stabilized



¹D. G. Matei et al., J. Phys. Conf. Ser., 723, 012031 (2016)

²D. G. Matei et al., PRL 118, 2632202 (2017)

By stabilizing the clock laser to a cryogenic silicon cavity^{1,2} (PTB), using a transfer-lock scheme

I-SOC clock demonstrator instability

Instability determined by comparison with ^{87}Sr clock at PTB^{1,2}

Combined instability of
the two clocks:

$$4.2 \times 10^{-16}/\sqrt{\tau}$$

Lowest instability:

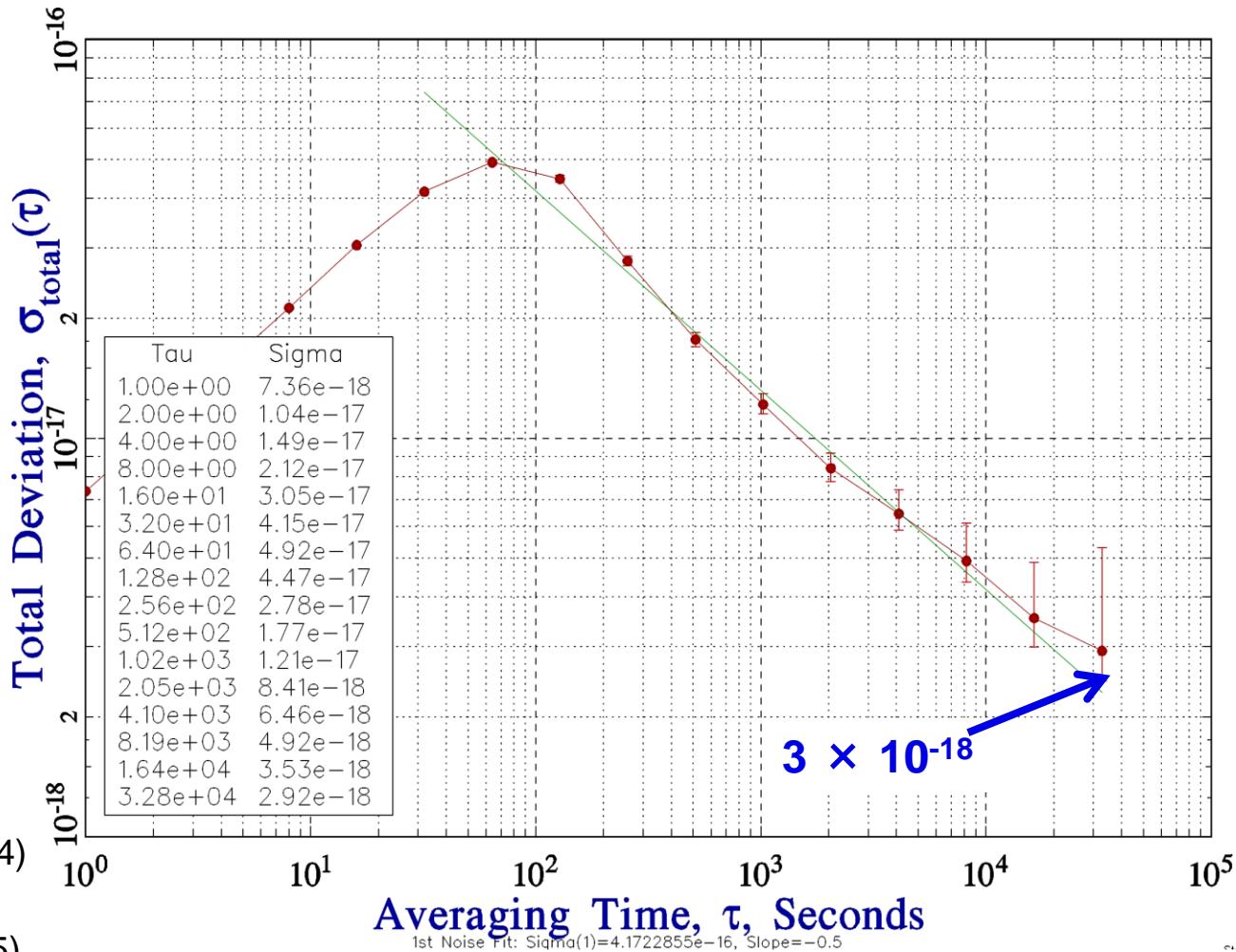
$$3 \times 10^{-18} \text{ at } \tau = 2 \times 10^4 \text{ s}$$

Tot. averaging time:
102 000 s

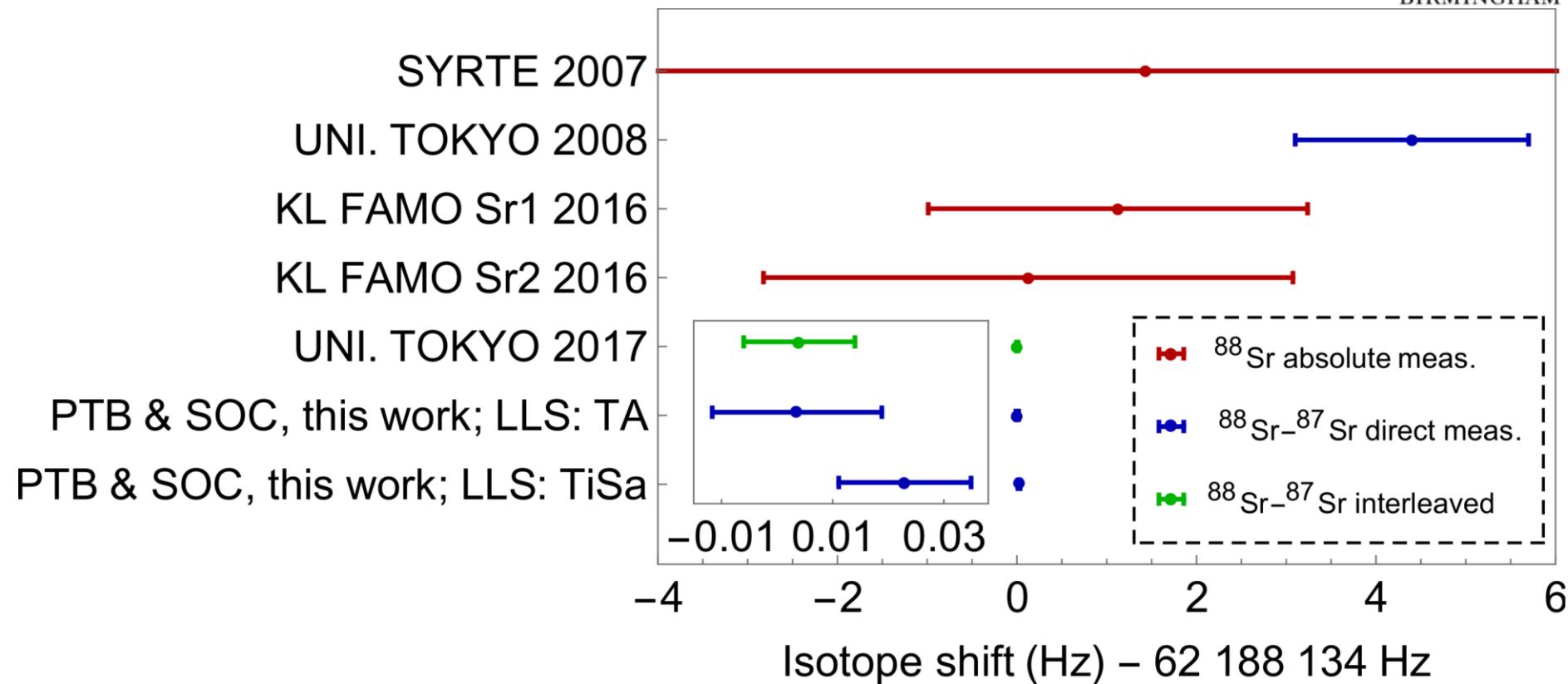
SOC clock locked
continuously to atoms
for **74 hours!**

¹S. Falke et al.,
New J. Phys. 16, 073023 (2014)

²A. Al-Masoudi et al.,
Phys. Rev. A 92, 063814 (2015)



I-SOC(^{88}Sr) and Sr-PTB(^{87}Sr)



- X. Baillard *et al.*, Opt. Lett. **32**, 1812 (2007)
T. Akatsuka *et al.*, Nature Phys. **4**, 954 (2008)
P. Morzynski *et al.*, Sci. Rep. **5**, 17495 (2015)
C. Radzewicz *et al.*, Phys. Scr. **91**, 084003 (2016)
T. Takano *et al.*, Appl. Phys. Expr. **10**, 072801 (2017)

- ▶ test system for components
- ▶ very good optical clock
- ▶ transportable clock laser...

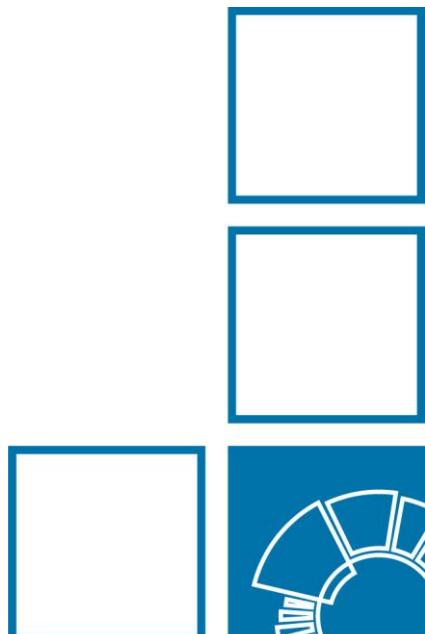
In conclusion:

- ▶ Optical clocks are pretty accurate/stable/cool.
We are getting closer to uncertainties of 10^{-18} .
- ▶ All fits into a car trailer,
low- 10^{-17} uncertainties have been demonstrated.
- ▶ Space seems possible!
Many building blocks are there (ACES, Lisa pathfinder, combs...)
- ▶ Why space?
many fundamental experiments are ‘easier’
a new SI-second will need intercontinental links
Earth observation: long-term stable height reference

Many thanks to:

Strontium:

J. Grotti
S. Koller
S. Herbers
S. Vogt
S. Dörscher
A. Al-Masoudi
R. Schwarz



Cavities & Combs:

S. Häfner
E. Benkler
D. Matei
T. Legero
U. Sterr

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